

Simulation of Wood Combustion in PATO Using a Detailed Pyrolysis Model Coupled to fireFoam

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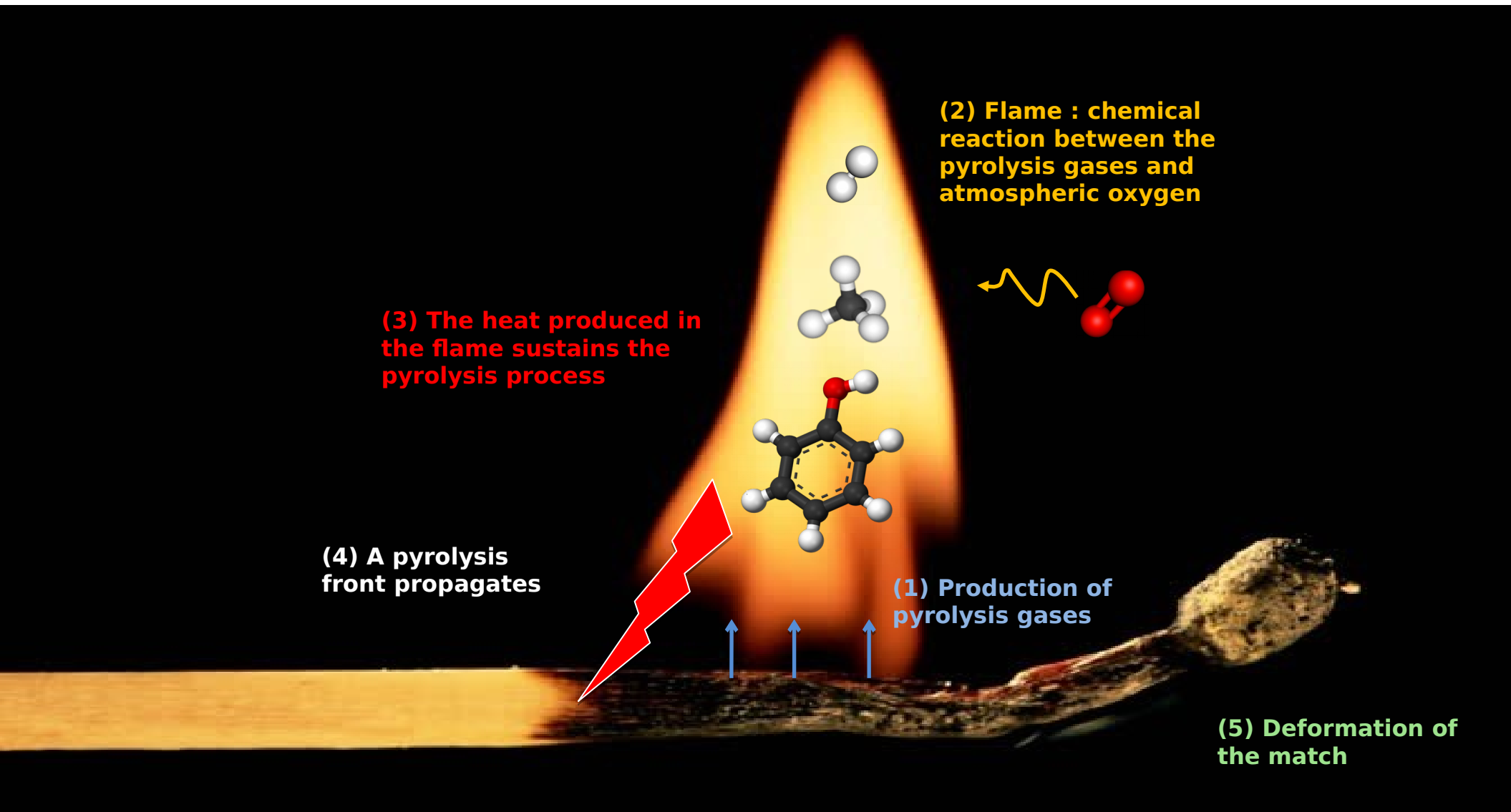
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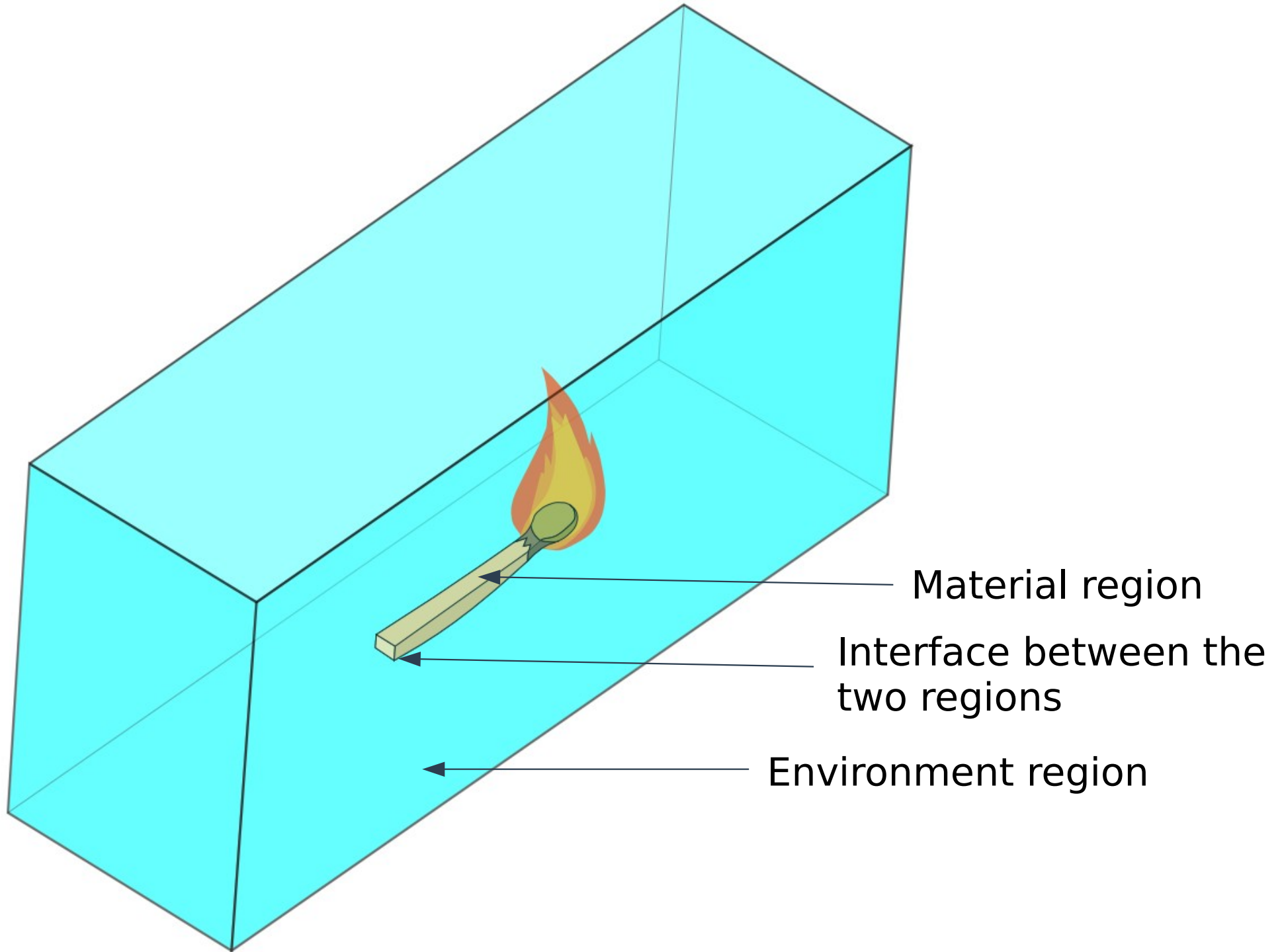
RESEARCH UNIT Institut de mécanique et d'ingénierie (I2M), Bordeaux

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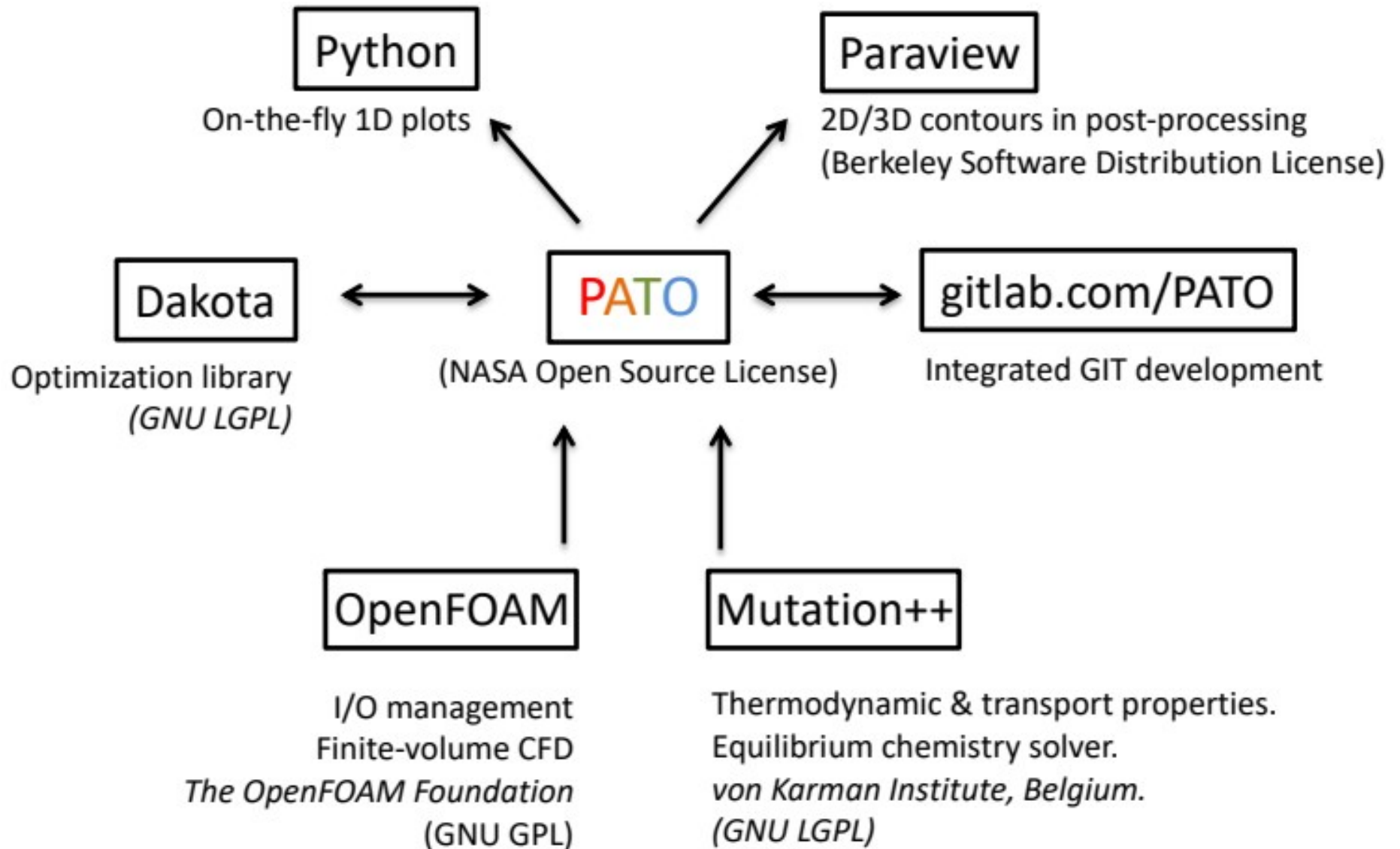
The Burning of a Match

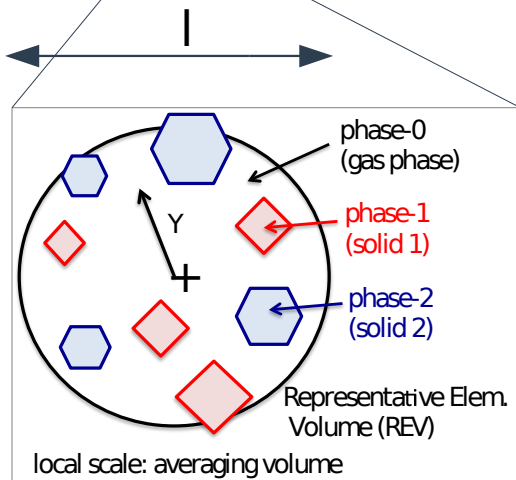
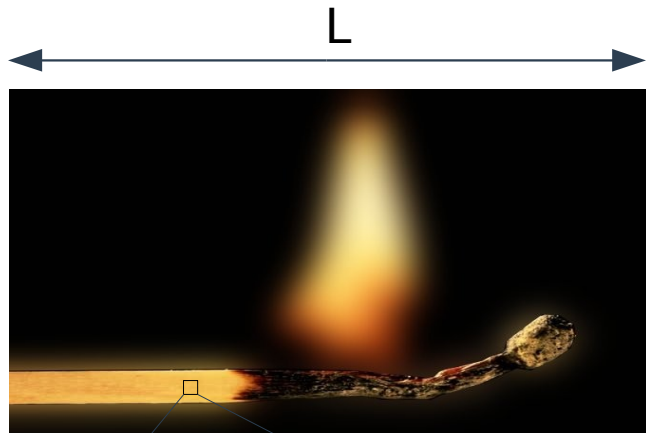
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POROUS MATERIAL ANALYSIS TOOLBOX BASED ON OPENFOAM





$$L \gg l$$

Averaged effective properties e.g. density

$$\rho = \epsilon_g \rho_g + \sum_{i \in [1, N_p]} \epsilon_i \rho_i$$

↑ volume fraction ↙ intrinsic phase density

Mass conservation

- For each solid phase

$$\partial_t(\epsilon_i \rho_i) = -\Pi_i - \Omega_i^h$$

density pyrolysis heterogeneous reactions

- For the gas phase

$$\partial_t(\epsilon_g \rho_g) + \partial_x \cdot (\epsilon_g \rho_g \mathbf{v}_g) = - \sum \partial_t(\epsilon_i \rho_i)$$

density convection exchange with solid phases

Species conservation

$$\partial_t(\epsilon_g \rho_g y_i) + \partial_x \cdot (\epsilon_g \rho_g y_i \mathbf{v}_g) + \partial_x \cdot \mathcal{F}_i = \pi_i + \epsilon_g \omega_i \mathcal{M}_i, \forall i \in N_g^s$$

species mass fractions convection diffusion pyrolysis chemistry gaseous species source terms

Momentum conservation

$$\mathbf{v}_g = -\frac{1}{\epsilon_g} \left(\frac{1}{\mu} \underline{\underline{\mathbf{K}}} + \frac{1}{p} \underline{\underline{\beta}} \right) \cdot \partial_x p$$

gas velocity Darcy Klinkenberg

Energy conservation

- solid

$$\sum_{i=1}^{N_p} [(\epsilon_i \rho_i C_{p,i}) \partial_t T_s] + \sum_{i=1}^{N_p} h_i \partial_t(\epsilon_i \rho_i) = \partial_x \cdot (\underline{\underline{K}}_s \cdot \partial_x T_s) + h_v(T_g - T_s)$$

- gas

$$(\epsilon_g \rho_g C_{p,g}) \partial_t T_g - \partial_t(\epsilon_g p) + \sum_{j=1}^{N_g} [h_j \partial_t(\epsilon_j \rho_j y_j) + \partial_x \cdot Q_j] + \partial_x \cdot (\epsilon_g \rho_g h_g \mathbf{v}_g) = \partial_x \cdot (\underline{\underline{K}}_g \cdot \partial_x T_g) + h_v(T_s - T_g)$$

energy term pressure species effective diffusion convection diffusion/viscous dissipation convective heat transfer

Solid deformation

$$\partial_t(\rho \partial_t \mathbf{D}) = \partial_x \cdot \underline{\underline{\sigma}} + \rho \mathbf{f}$$

displacement stress tensor body forces



Navier-Stokes equations with LES filtering and Favre mean variables

$$\bar{\Phi} \equiv \frac{1}{T} \int_T \Phi(t) dt$$

$$\tilde{\Phi} \equiv \frac{\bar{\rho}\Phi}{\bar{\rho}}$$

Mass conservation

$$\partial_t(\bar{\rho}) + \nabla \cdot (\bar{\rho} \tilde{\mathbf{u}}) = 0$$

density velocity

Momentum conservation

$$\partial_t(\bar{\rho} \tilde{\mathbf{u}}) + \nabla \cdot (\bar{\rho} \tilde{\mathbf{u}} \tilde{\mathbf{u}}) = -\nabla \bar{p}_m - (\mathbf{g} \cdot \mathbf{x}) \nabla \bar{\rho} + \nabla \cdot [\mu_{eff} (\nabla \tilde{\mathbf{u}} + (\nabla \tilde{\mathbf{u}})^T - \frac{2}{3} (\nabla \cdot \tilde{\mathbf{u}}) \mathbf{I})]$$

modified pressure position effective viscosity

$$\bar{p}_m = \bar{p} - \bar{\rho} \mathbf{g} \cdot \mathbf{x}$$

thermodynamic pressure

$$\mu_{eff} = \mu_{sgs} + \mu$$

sub-grid viscosity

dynamic viscosity

Species transport equations

$$\partial_t(\bar{\rho} \tilde{Y}_i) + \nabla \cdot (\bar{\rho} \tilde{\mathbf{u}} \tilde{Y}_i) = \nabla \cdot (\bar{\rho} D_{eff} \nabla \tilde{Y}_i) + \bar{w}_i$$

i-th specie mass fraction effective mass diffusivity

rate of production of a specie

Energy conservation

$$\partial_t(\bar{\rho} \tilde{h}_s) + \nabla \cdot (\bar{\rho} \tilde{\mathbf{u}} \tilde{h}_s) = \partial_t \bar{p} + \tilde{\mathbf{u}} \cdot \nabla \bar{p} + \nabla \cdot (\bar{\rho} \alpha_{eff} \nabla \tilde{h}_s) + \bar{Q}_c - \nabla \cdot \bar{\mathbf{q}}_R$$

sensible enthalpy Effective thermal diffusivity

heat generated by combustion

thermal radiation flux

Ideal gas

$$\bar{\rho} = \frac{\bar{p} M}{R \bar{T}}$$

Molar weight temperature

$$M = \left[\frac{\sum_{i=1}^N \tilde{Y}_i}{M_i} \right]^{-1}$$

$$\tilde{h}_s = \sum_{i=1}^N \tilde{Y}_i h_{s,i}(\tilde{T})$$

$$h_{s,i}(\tilde{T}) = h_{s,i}^{ref} + \int_{T^{ref}}^{\tilde{T}} C_{P,i}^0 dT$$

constant-pressure specific heat

JANAF model

$$C_{P,i}^0 = R \left[\frac{a_1}{T^2} + \frac{a_2}{T} + a_3 + a_4 T + a_5 T^2 + a_6 T^3 + a_7 T^4 \right]$$

Sutherland model

$$\mu = \frac{C_1 T^{3/2}}{T + C_2}$$

+ **Combustion model** (\bar{Q}_C)

+ **Turbulence model** ($\mu_{sgs}, \alpha_{sgs}, D_{sgs}$)

+ **Radiation model** ($\bar{\mathbf{q}}_R$)



f = environment
g = material

Velocity

$$\tilde{\mathbf{u}}_f = \mathbf{u}_g$$

Pressure

$$\bar{p}_f = p_g$$

Species concentration (y)

- if flux from the environment to the material

$$y_{i,g} = \tilde{y}_{i,f}$$

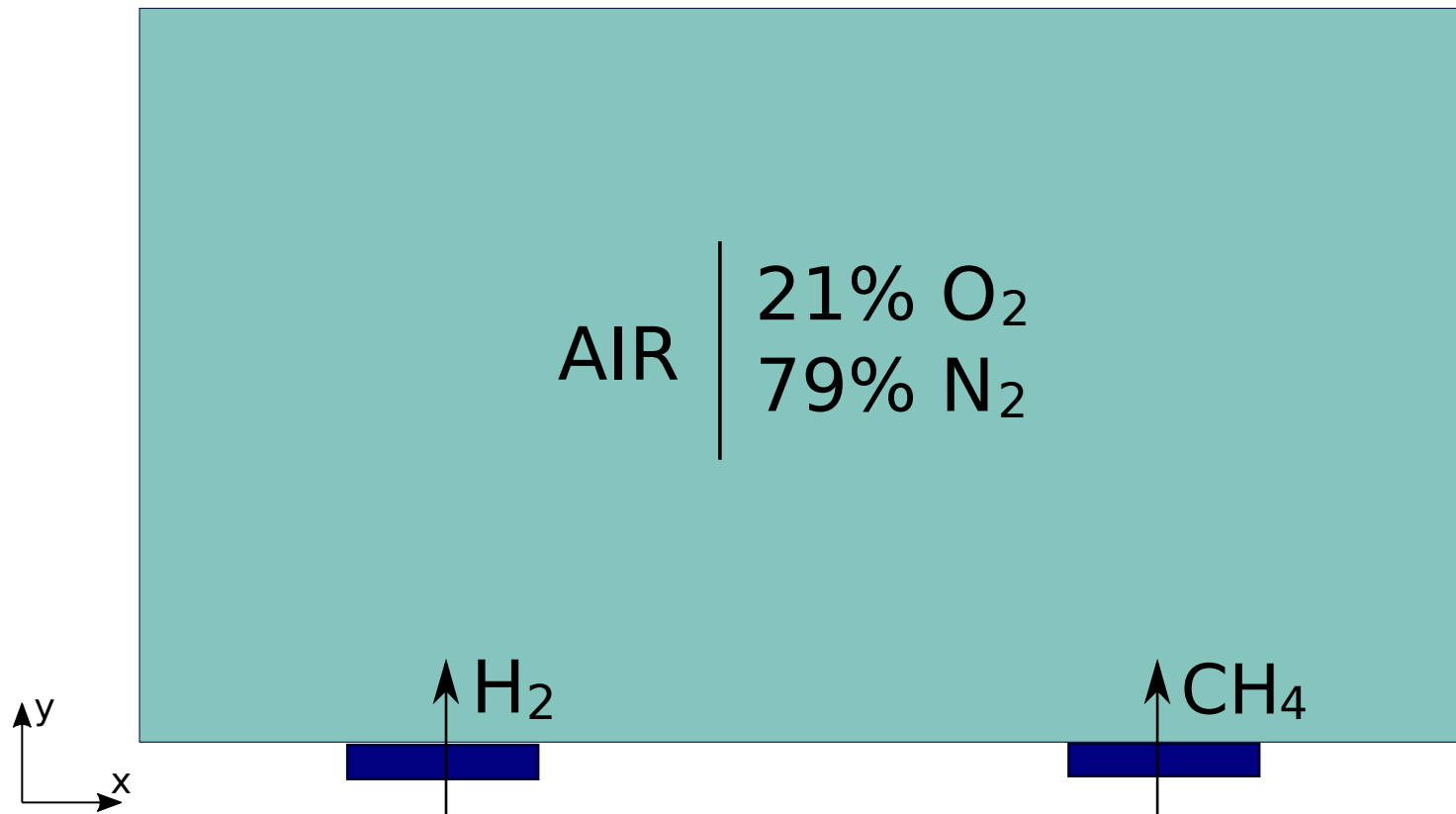
- if flux from the material to the environment

$$\tilde{y}_{i,f} = y_{i,g}$$

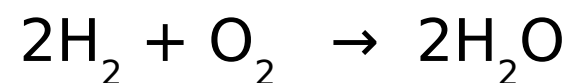
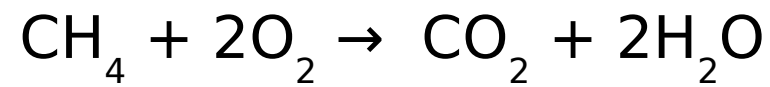
Temperature

$$\tilde{T}_f = T_g$$

$$k_f \nabla \tilde{T}_f = k_g \nabla T_g$$



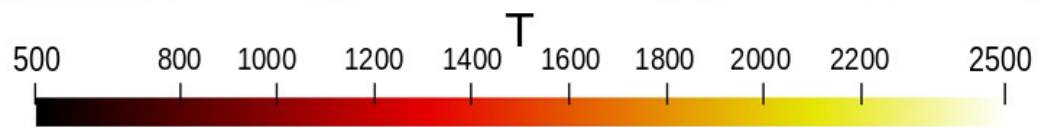
Combustion reactions



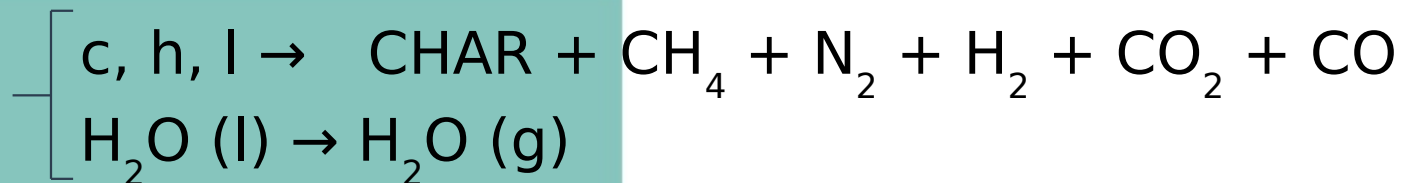
Time: 8.0 s

Time: 8.2 s

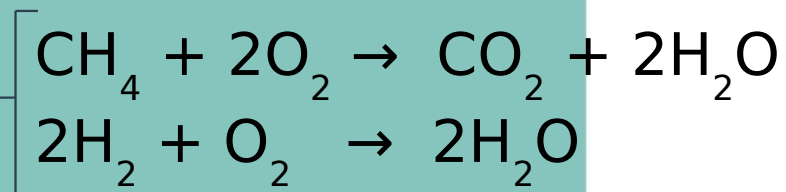
Time: 8.4 s



Pyrolysis reactions

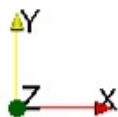


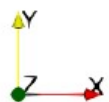
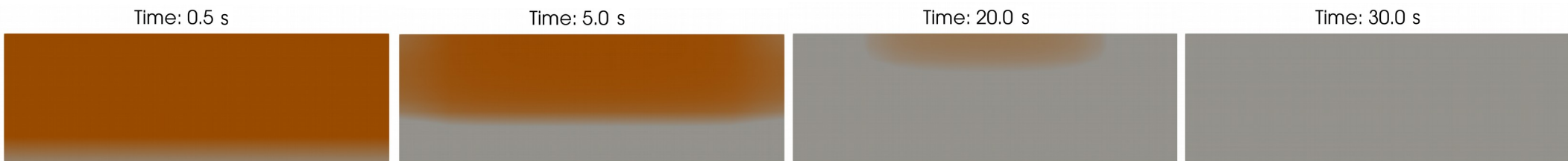
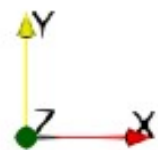
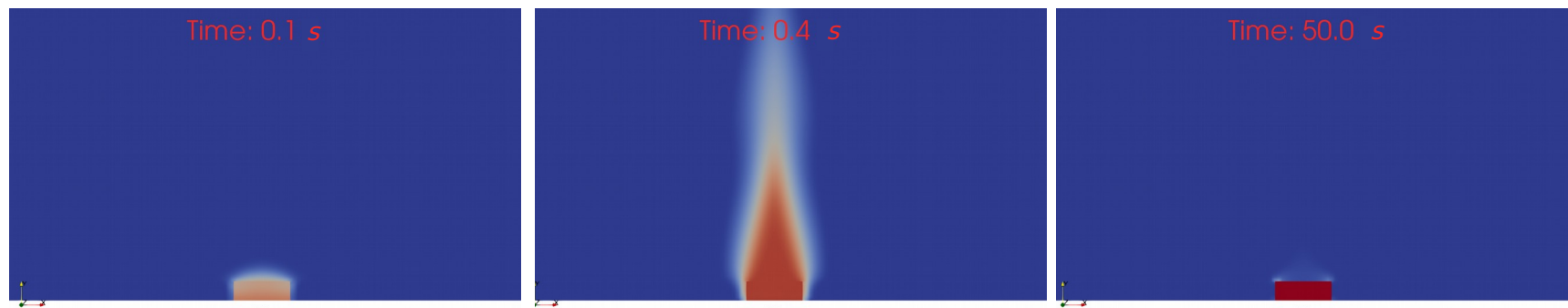
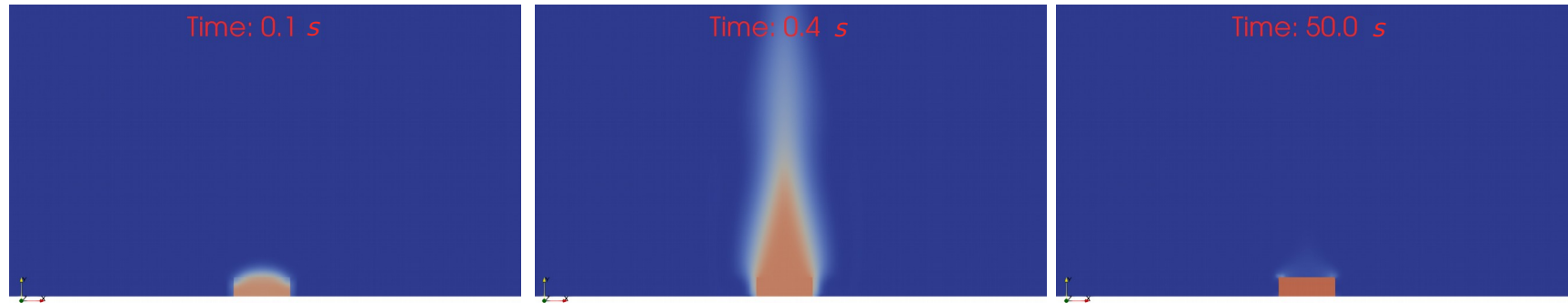
Combustion reactions



air $\left\{ \begin{array}{l} 29\% \text{ O}_2 \\ 71\% \text{ N}_2 \end{array} \right.$

wood $(\epsilon_w=0.5)$ $\left\{ \begin{array}{l} 28\% \text{ hemicellulose} \\ 18\% \text{ lignin} \\ 44\% \text{ cellulose} \\ 10\% \text{ water} \end{array} \right.$





Main Goal

Define a numerical tool to deal with this multi-physical problem.

Numerical tool

PATO: detailed porous material solver coupled to several OpenFoam flow solvers, including FireFoam

A First Application

Numerical simulation of a log combustion.

Future Works

- Extend the application by considering solid deformation;
- Extend the application to 3D;
- Apply the solver to the Burning of the match;

THANK YOU

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